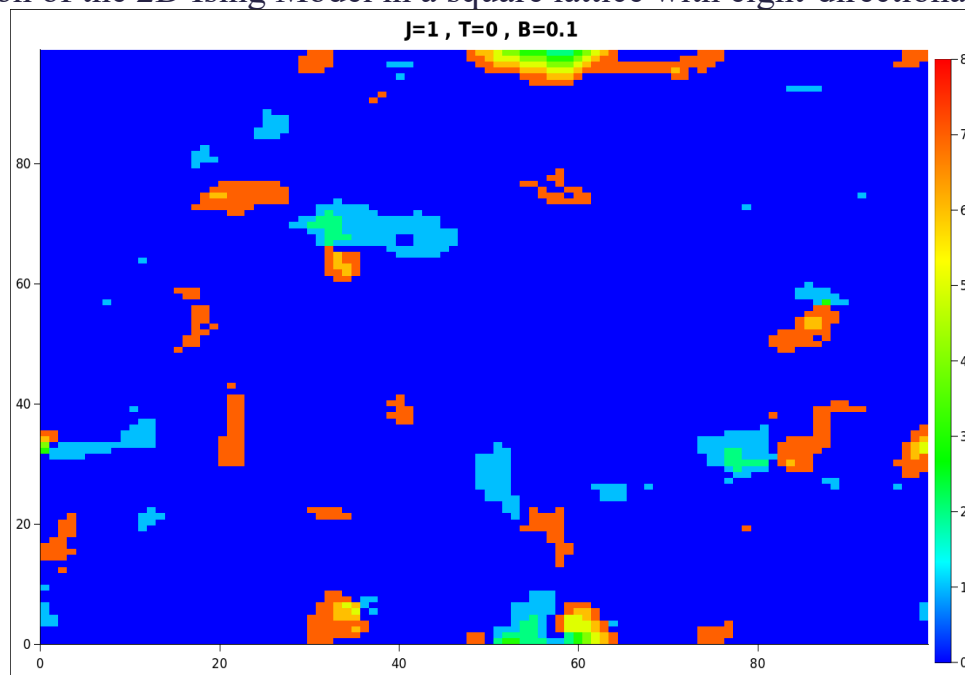


## Simulation of the 2D Ising Model in a square lattice with eight-directional Spin



```
#include <fstream>
```

```
#include <cmath>
```

```
#include <stdlib.h>
```

```
#include <ctime>
```

```
using namespace std;
```

```
const int N = 100;
```

```
const float J = 1.0, T = 2.0, h = 5.0; // h is the external magnetic field
```

```
const int directions = 8; // 8 directions: up, down, left, right, and the four diagonals
```

```
int main(){
```

```
    srand(time(NULL));
```

```
    int S[N][N];
```

```
    float Ei,Ef,deltaE;
```

```
    float r;
```

```

int i,j;

int ii,jj;

float Smeanx,Smeany,Emean;

float angle[directions]={0,M_PI/4,M_PI/2,3*M_PI/4,M_PI,5*M_PI/4,3*M_PI/2,7*M_PI/4}; //
// directions are in radians

// directions are in radians
for(i=0;i<N;i++){
    for(j=0;j<N;j++){
        S[i][j]=rand()%directions;
    }
}

ofstream outs("sdata(t=2,h=5).txt");
ofstream outc("sconfig(t=2,h=5).txt");

for(int n=0;n<1000000;n++){
    Ei=0.0;
    for(i=0;i<N;i++){
        for(j=0;j<N;j++){
            Ei+=-J*0.5*cos(angle[S[i][j]]-angle[S[(i+1)%N][j]])-J*0.5*cos(angle[S[i][j]]-angle[S[i][(j+1)%N]])-
            J*0.5*cos(angle[S[i][j]]-angle[S[(i-1+N)%N][j]])-J*0.5*cos(angle[S[i][j]]-angle[S[i][(j-1+N)%N]])-
            h*cos(angle[S[i][j]]); // directions are in radians
        }
    }

    ii=rand()%N;
    jj=rand()%N;
    int old_S=S[ii][jj];

```

```

S[ii][jj]=rand()%directions; // 0° to 360°
deltaE=0.0;
for(i=0;i<N;i++){
  for(j=0;j<N;j++){
    Ef+=-J*0.5*cos(angle[S[i][j]]-angle[S[(i+1)%N][j]])-J*0.5*cos(angle[S[i][j]]-angle[S[i][(j+1)%N]])-
    J*0.5*cos(angle[S[i][j]]-angle[S[(i-1)%N][j]])-J*0.5*cos(angle[S[i][j]]-angle[S[i][(j-1)%N]])-
    h*cos(angle[S[i][j]]); // 0 to 1
  }
}
deltaE=Ef-Ei;
if(deltaE>0){
  r=rand()/(RAND_MAX+1.0);
  if(r>exp(-deltaE/T)){
    S[ii][jj]=old_S; // 0 to 360°
    Emean=Ei/(N*N);
  }else{
    Emean=Ef/(N*N);
  }
}else{
  Emean=Ef/(N*N); // 0 to 360°
}

Smeanx=0.0;
Smeany=0.0;
for(i=0;i<N;i++){
  for(j=0;j<N;j++){
    Smeanx+=cos(angle[S[i][j]]);
    Smeany+=sin(angle[S[i][j]]);
  }
}

```

```
    }
    Smeanx/=(N*N);
    Smeany/=(N*N);
    outs<<n<<'\t'<<Emean<<'\t'<<Smeanx<<'\t'<<Smeany<<'\n';
}

outs.close();

for(i=0;i<N;i++){
    for(j=0;j<N;j++){
        outc<<i<<'\t'<<j<<'\t'<<S[i][j]<<'\n';
    }
}

outc.close();

return 0;
}
```